

# Compositional Symbolic Execution through Program Specialization

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## Software Testing and Test Data Generation

- ▶ Quality assurance
- ▶ Software testing
- ▶ Automated test data generation
- ▶ Wide variety of approaches to test data generation
- ▶ Symbolic execution (SPF, Symbolic PathFinder)
  - ▶ High cost of symbolic execution on large programs
    - ▶ Large (possibly infinite) number of execution paths
    - ▶ Size of their associated constraint sets
  - ▶ Additional complexity to handle arbitrary data structures
  - ▶ [babelfish.arc.nasa.gov/trac/jpf/wiki/projects/jpf-symbolc](http://babelfish.arc.nasa.gov/trac/jpf/wiki/projects/jpf-symbolc)

## Our approach



- ▶ Scalability towards handling realistic programs
- ▶ Compositional reasoning in **SPF** (on top of **JPF**, Java PathFinder)
- ▶ Generation and re-utilization of method summaries to scale up
- ▶ Leveraging program specialization

## Symbolic Execution

- ▶ King [Comm. ACM 1976], Clarke [IEEE TSE 1976]
- ▶ Analysis of programs with unspecified inputs
- ▶ Symbolic states represent sets of concrete states
  - ▶ symbolic values/expressions for variables
  - ▶ Path condition
  - ▶ Program counter
- ▶ For each path, build path condition
  - ▶ condition on inputs, for the execution to follow that path
  - ▶ check path condition satisfiability, explore only feasible paths

# Symbolic Execution

- ▶ Renewed interest in recent years
- ▶ Applications: test-case generation, error detection,...
- ▶ Tools
  - ▶ CUTE and jCUTE (UIUC)
  - ▶ EXE and KLEE (Stanford)
  - ▶ CREST and BitBlaze (UC Berkeley)
  - ▶ Pex, SAGE, YOGI and PREFIX (Microsoft)
  - ▶ **Symbolic Pathfinder (NASA)**
  - ▶ ...

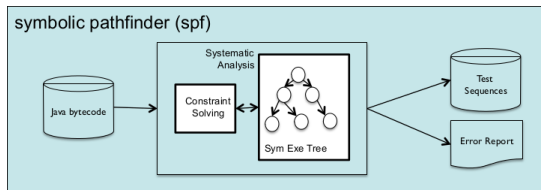
# Program Specialization

- ▶ Partial Evaluation and Automatic Program Generation [Jones, 1993]
- ▶ Partial evaluation creates a specialized version of a general program

```
int f(n,x) {  
  if (n == 0)  
    return 1;  
  else  
    if (even(n))  
      return pow(f(n/2,x),2);  
    else  
      return x * f(n-1,x);  
}  
  
f3(x) {  
  return x * pow(x * 1,2);  
}
```

- ▶ Main benefit
  - ▶ speed of execution
  - ▶ specialized program faster than general program
- ▶ Some applications: compiler optimization, program transformation

## Symbolic PathFinder (SPF)



- ▶ Built on top of JPF (<http://babelfish.arc.nasa.gov/trac/jpf/>)
- ▶ SPF combines symbolic execution, model checking and constraint solving for test case generation
- ▶ Handles dynamic data structures, loops, recursion, multi-threading, arrays, strings,... [TACAS 2003, ISSTA 2008, ASE 2010]

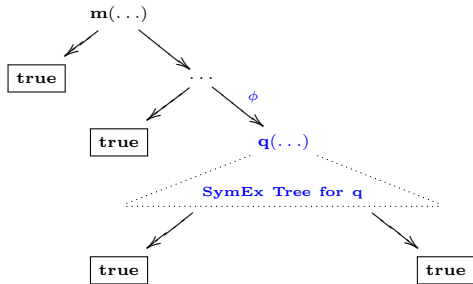
# Symbolic PathFinder (SPF)

## Symbolic PathFinder (SPF) - Implementation

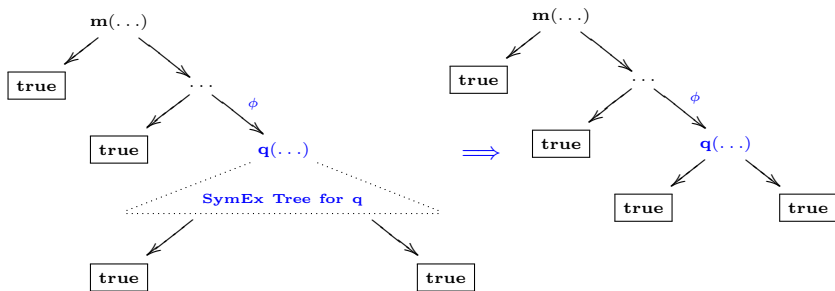
- ▶ Non-standard interpreter of byte-codes
  - ▶ Symbolic execution replaces concrete execution semantics
  - ▶ Enables JPF to perform systematic symbolic analysis
- ▶ Lazy Initialization for arbitrary input data structures
  - ▶ Non-determinism handles aliasing
  - ▶ Different heap configurations explored explicitly
- ▶ Attributes store symbolic information
- ▶ Choice generators
  - ▶ Non-deterministic choices in branching conditions
- ▶ Listeners
  - ▶ Influence the search, collect and print results
- ▶ Bounded exploration to handle loops



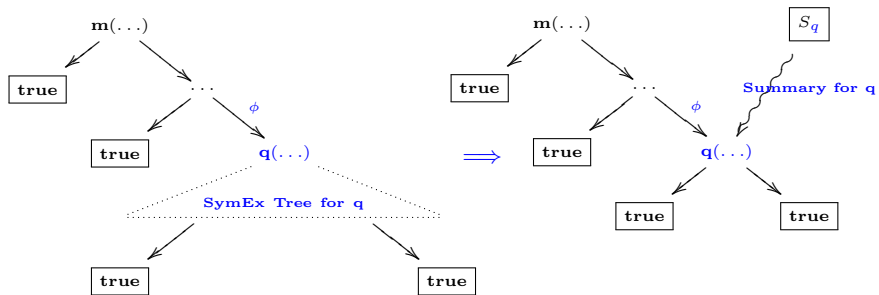
# Compositional Symbolic Execution



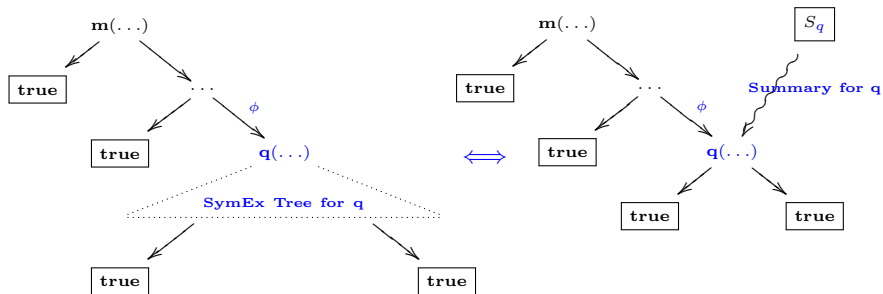
# Compositional Symbolic Execution



# Compositional Symbolic Execution



# Compositional Symbolic Execution



## Composition

- ▶ Compatibility check between summary cases of  $q$  and current state of  $m$
- ▶ Only compatible summary cases are composed
- ▶ Summary cases's path constraints are conjoined with current state
- ▶ Summary for method  $m$  is created

# Compositional Symbolic Execution

- ▶ Challenge
  - ▶ Composition in the presence of heap operations
- ▶ Previous approaches
  - ▶ Explicit representation of input and output heap [Albert et al., LOPSTR'10]
    - ▶ Potentially expensive, not natural in SPF
  - ▶ Summarize program as logical disjunctions [Godefroid, POPL'07]
    - ▶ No treatment of the heap
- ▶ Our approach
  - ▶ Leverage partial evaluation to build method summaries
  - ▶ Summaries are specialized versions of method code
  - ▶ Used to reconstruct the heap

## Method Summaries

A method summary is a set of tuples of the form:

$$\langle \mathbf{PC}, \mathbf{HeapPC}, \mathbf{SpC}, \mathbf{CmpSch} \rangle$$

where:

- ▶ **PC**: Path Condition
  - ▶ Conjunction of constraints over symbolic inputs
  - ▶ Generated from conditional statements (`if`, `if_icmpeq`, etc.)
- ▶ **HeapPC**: Heap Path Condition
  - ▶ Conjunction of constraints over the heap
  - ▶ Generated via lazy initialization (`aload`, `getfield`, `getstatic`)
- ▶ **SpC**: Specialized Code
  - ▶ Sequence of byte-codes executed along a specific path
  - ▶ Does not contain conditional statements
- ▶ **CmpSch**: Composition schedule
  - ▶ For each `invoke` instruction, determines which case from the invoked method's summary to compose
  - ▶ Incremental, deterministic composition of method summaries

# Method Summaries

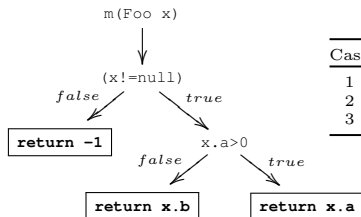
## Java source code

```
int m(Foo x) {  
    if (x != null)  
        if (x.a > 0)  
            return x.a;  
        else  
            return x.b;  
    else return -1;  
}
```

## Java bytecode

```
0: aload x  
1: ifnull 11  
2: aload x  
3: getfield a  
4: ifle 8  
5: aload x  
6: getfield a  
7: ireturn  
8: aload x  
9: getfield b  
10: ireturn  
11: iconst -1  
12: ireturn
```

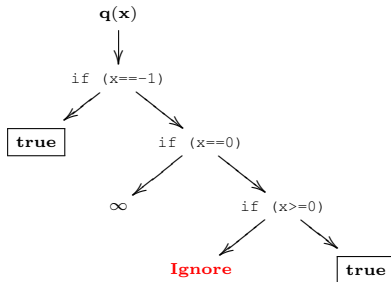
## Symbolic Execution



## Method summary

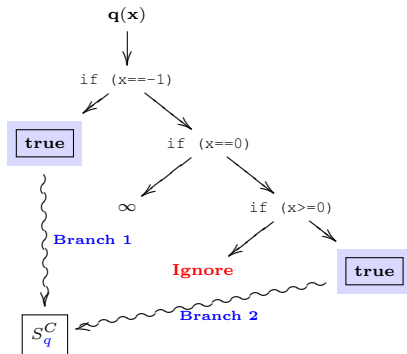
Case	PC	HeapPC	Code
1	$\emptyset$	$\{x = \text{null}\}$	[iconst -1, ireturn]
2	$\{x.a > 0\}$	$\{x \neq \text{null}\}$	[aload x, getfield a, ireturn]
3	$\{x.a \leq 0\}$	$\{x \neq \text{null}\}$	[aload x, getfield b, ireturn]

## Generating Summaries

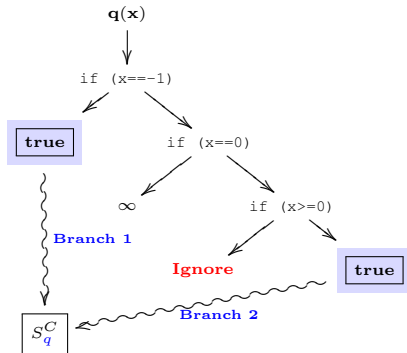




# Generating Summaries



# Generating Summaries



- ▶ The execution tree to be traversed is in general infinite. A termination criterion is needed
- ▶ A summary is a finite representation of the symbolic execution tree
- ▶ Complete for the given termination criterion, but Partial, in general
- ▶ Each element in a summary is said to be a (test) case of method  $q$

# Generating Summaries

## Specialization Algorithm

**Input:** `insn:Instruction`, `currentState`  $\equiv$   $\langle pc, hpc, code, sched \rangle$

**procedure** SPECIALIZATION

**switch** TYPE(`insn`) **do**

**case** ConditionalInstruction

`code`  $\leftarrow$  SLICECODE(`code`,`insn`)

**case** InvokeInstruction

COMPOSESUMMARY(`getInvokedMethod`(`insn`),`duringSP`)

`code`  $\leftarrow$  APPEND(`code`,`insn`)

**case** ReturnInstruction

`code`  $\leftarrow$  APPEND(`code`,`insn`)

STORESUMMARYCASE(`pc`,`hpc`,`code`,`sched`)

**case** GotoInstruction

IGNORE

**default**

`code`  $\leftarrow$  APPEND(`code`,`insn`)

**end procedure**

# Generating Summaries

## Example of Program Specialization

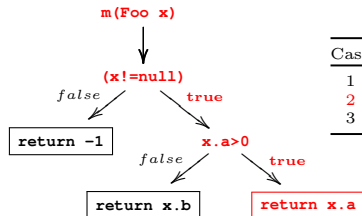
### Java source code

```
int m(Foo x) {  
    if (x != null)  
        if (x.a > 0)  
            return x.a;  
        else  
            return x.b;  
    else return -1;  
}
```

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9: getfield b  
10: ireturn  
11: iconst -1  
12: ireturn
```

### Symbolic Execution



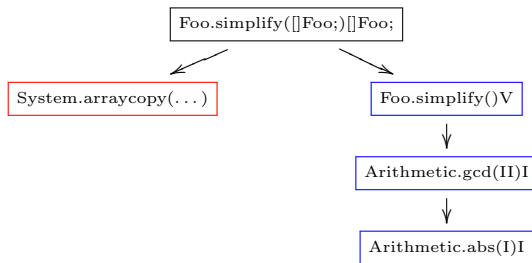
### Method summary

Case	PC	HeapPC	Code
1	$\emptyset$	$\{x = null\}$	[iconst -1, ireturn]
2	$\{x.a > 0\}$	$\{x \neq null\}$	[ <b>aload x, getfield a, ireturn</b> ]
3	$\{x.a \leq 0\}$	$\{x \neq null\}$	[ <b>aload x, getfield b, ireturn</b> ]

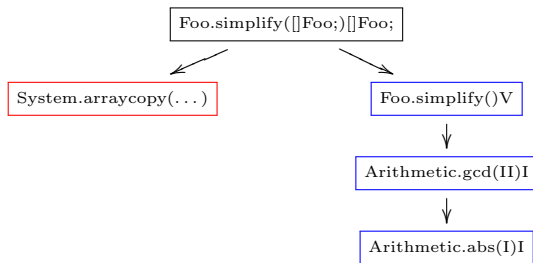
# Composition Strategy



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# Composition Strategy

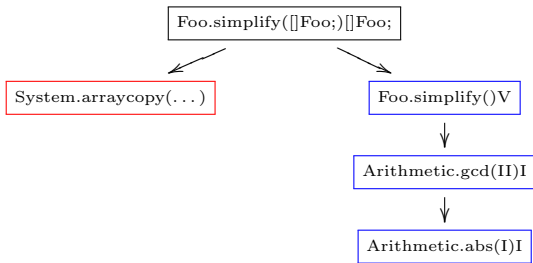


## Context-sensitive

**Pros.** Only required information is computed

**Cons.** Reusability of summaries is not always possible

# Composition Strategy



## Context-sensitive

**Pros.** Only required information is computed

**Cons.** Reusability of summaries is not always possible

## Context-insensitive

**Pros.** Composition can always be performed

**Cons.** Summaries can contain more cases than necessary (more expensive)



## Composition Algorithm

```
1: procedure COMPOSESUMMARY(m,mode)
2:   if mode = duringSP then
3:      $\mathcal{S} \leftarrow \text{getSummary}(m)$ 
4:     for all case  $\in \mathcal{S}$  do
5:       SETCOMPOSITIONSCHEDULE(case.getCompSched())
6:       COMPOSECASE(case)
7:     end for
8:   else
9:      $\mathcal{S} \leftarrow \text{getSummary}(m)$ 
10:    caseIndex  $\leftarrow \text{compositionSchedule.getNext}()$ 
11:    case  $\leftarrow \text{getSummaryCase}(\mathcal{S},\text{caseIndex})$ 
12:    COMPOSECASE(case)
13:   end if
14: end procedure
```

## Composition Algorithm

```
1: procedure COMPOSECASE(case)
2:   heapPC  $\leftarrow$  case.getHeapPC()
3:   PROJECTACTUALPARAMETERS(heapPC)
4:   if CHECKANDSET(currentHeapPC,heapPC) then
5:     pc  $\leftarrow$  case.getPC()
6:     PROJECTACTUALPARAMETERS(pc)
7:     currentPC  $\leftarrow$  currentPC  $\cup$  pc
8:     if SATISFY(currentPC) then
9:       REPLACECODE(invokedMethod,case.getCode())
10:      CONTINUESYMBOLICEXECUTION  $\triangleright$  mode  $\neq$  duringSP
11:    else
12:      BACKTRACK
13:    end if
14:  else
15:    BACKTRACK
16:  end if
17: end procedure
```

# Composition Algorithm

## Example of Summary Composition

```
int abs(int a){
    if (a >= 0) return a;
    else return -a;
}
int q(Foo x){
    if (x != null && x.next != null
        && x.next.next != null
        && x.next.next.f != 0)
        return abs(x.next.f);
    else
        ...
}

void m(Foo x, Foo y, Foo z){
    Foo[] arr = new Foo[]{x,y,z};
    for (int i=0; i<arr.length; i++){
        if (arr[i] != null)
            arr[i].f = q(arr[i]);
        else
            ...
    }
}
```

Case	PC	HeapPC	Code	Sched
Method abs				
0	$\{a \geq 0\}$	$\emptyset$	[iload a, ireturn]	[]
1	$\{a < 0\}$	$\emptyset$	[iload a, neg, ireturn]	[]
Method q				
...				
6	$\{x.f \geq 0, x.f \neq 0\}$	$\{x \neq null, x.next = x\}$	[aload x, getfield next, getfield next, [0] getfield f, invoke abs, ireturn]	[0]
...				
Method m				
...				
22	$\{z.f \geq 0, z.f \neq 0\}$	$\{x = null, y = null$ $z \neq null, z.next = z\}$	[..., invoke q, ...]	[6, 0]
...				

# Implementation

- ▶ Specialization Listener
  - ▶ Slice code for conditional instructions (`if`, `if_icmpeq`, `ifnull`, ...)
  - ▶ Invoke instructions: Update specialized code, compose summary
  - ▶ Return instructions: Update specialized code and store summary case
  - ▶ Ignore `goto` instructions
  - ▶ For the remaining instructions, append instruction to specialized code
- ▶ Compositional Listener
  - ▶ Execute composition algorithm
- ▶ Other new classes: `MethodSummary`, `MethodSummaryCase`, `SpecializedCode`, `BindingMap`, `CompositionSchedule`, `NewSummaryChoiceGenerator`, `CompositionChoiceGenerator`
- ▶ Optimized conditional bytecode instructions

# Experience

Example featuring linear integer constraints

Java source code

```
public static int abs(int x){
    if (x >= 0) return x;
    else return -x;
}
public static int gcd(int x, int y) {
    if (x == 0) return abs(y);
    while ((y != 0) && (i < 2)) {
        if (x > y) x = x-y;
        else y = y-x;
        if (i==2) return -1;
        i++;
    }
    return abs(x);
}
public class R{
    private int num, den;
    public void simplify(int a, int b){
        int gcd = gcd(a,b);
        if (gcd != 0) {
            num = num/gcd; den = den/gcd;
        }
    }
    public static R[] simp(R[] rs){
        R[] oldRs = new R[rs.length];
        arraycopy(rs,oldRs,length);
        for (int i = 0; i < length; i++)
            rs[i].simplify(rs[i].num,rs[i].den);
        return oldRs;
    }
}
```

## Preliminary Experimental Results

Number of summary cases

Method abs: 2  
Method gcd: 13  
Method simplify: 14  
Method simp: 2744

SPF vs. Compositional SPF

	SPF	CompSPF
Time	00:02:50	00:01:02
States	24899	13928
Choice Generators	12449	5689
Instructions	145908	139992
Max. Memory	106MB	170MB

# Experience

Example featuring input data structures to stress lazy initialization

```
public int q(Foo x, Foo y){
    if (x != null) {
        if ((x.next != null) &&
            (x.next.next != null) &&
            (x.next.next.next != null) &&
            (x.next.next.next.f == 0))
            return -1;
        else
            return 0;
    } else if ((y != null) &&
               (y.next != null) &&
               (y.next.f == 0))
        return 1;
    else
        return 2;
}

public void m(Foo x, Foo y, Foo z){
    Foo[] arr = new Foo[]{x,y,z};
    for (int i=0; i < arr.length; i++) {
        if (arr[i] != null)
            arr[i].f = q(arr[i],y);
        else
            arr[i] = new Foo(0,0);
    }
}
```

## Preliminary Experimental Results

Number of summary cases

Method q: 22

Method m: 9938

SPF vs. Compositional SPF

	SPF	CompSPF
Time	00:00:51	00:00:13
States	86175	27762
Choice Generators	29550	1215
Instructions	1215959	223786
Max. Memory	242MB	364MB

## Related Work

### Compositional symbolic execution

- ▶ Compositional dynamic test generation [Godefroid, POPL'07]
- ▶ Demand-driven compositional symbolic execution [Anand et al., TACAS'08]
- ▶ Compositional test case generation in CLP [Albert et al., LOPSTR'10]
- ▶ Theoretical aspects of compositional symbolic execution [Vanoverberghe et al., FASE'11]

### Symbolic execution and program specialization

- ▶ Software specialization via symbolic execution [Coen-Porisini et al., IEEE TSE'91]
- ▶ Interleaving symbolic execution and partial evaluation [Bubel et al., FMCO'10]

## Conclusions and Future Work

- ▶ Compositional reasoning based on partial evaluation
  - ▶ alleviate scalability problems in Symbolic Execution for Software Testing
- ▶ Implementation in SPF
- ▶ Practical issues:
  - ▶ Validate and optimize implementation
  - ▶ Full integration in SPF
  - ▶ Experimental evaluation
- ▶ Optimization
  - ▶ Constraints simplification
  - ▶ Save sequence instruction indexes in the specialized code
- ▶ Proofs of correctness
- ▶ Multi-threaded Java programs
- ▶ Focus on error detection



Thank you!