Formally Verified EVM Block-Optimizations*

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Abstract. The efficiency and the security of *smart contracts* are their two fundamental properties, but might come at odds: the use of optimizers to enhance efficiency may introduce bugs and compromise security. Our focus is on EVM (Ethereum Virtual Machine) *block-optimizations*, which enhance the efficiency of jump-free blocks of opcodes by eliminating, reordering and even changing the original opcodes. We reconcile efficiency and security by providing the verification technology to formally prove the correctness of EVM block-optimizations on smart contracts using the Coq proof assistant. This amounts to the challenging problem of proving semantic equivalence of two blocks of EVM instructions, which is realized by means of three novel Coq components: a symbolic execution engine which can execute an EVM block and produce a symbolic state; a number of simplification lemmas which transform a symbolic state into an equivalent one; and a checker of symbolic states to compare the symbolic states produced for the two EVM blocks under comparison.

1 Introduction

In many contexts, security requirements are critical and formal verification today plays an essential role to verify/certify these requirements. One of such contexts is the blockchain, in which software bugs on smart contracts have already caused several high profile attacks (e.g., [16,15,28,35,14,13]). There is hence huge interest and investment in guaranteeing their correctness, e.g., Certora [1], Veridise [2], apriorit [3], Consensys [4], Dedaub [5] are companies that offer smart contract audits using formal methods' technology. In this context, efficiency is of high relevance as well, as deploying and executing smart contracts has a cost (in the corresponding cryptocurrency). Hence, optimization tools for smart contracts have emerged in the last few years (e.g., ebso [27], SYRUP [11], GASOL [10], the solc optimizer [9]). Unfortunately, there is a dichotomy of efficiency and correctness: as optimizers can be rather complex tools (not formally verified), they might introduce bugs and potential users might be reluctant of optimizing their code. This has a number of disruptive consequences: owners will pay more to deploy (non-optimized) smart contracts; clients will pay more to run transactions every time they are executed; the blockchain will accept less transactions as they are more costly. Rather than accepting such a dichotomy, our work tries to

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overturn it by developing a fully automated formal verification tool for proving the correctness of the optimized code.

The general problem addressed by the paper is formally verifying semantic equivalence of two bytecode programs, an initial code I and an optimization of it 0 —what is considered a great challenge in formal verification. For our purpose, we will narrow down the problem by (1) considering fragments of code that are jump-free (i.e., they do not have loops nor branching), and by (2) considering only stack EVM operations (memory/storage opcodes and other blockchainspecific opcodes are not considered). These assumptions are realistic as working on jump-free blocks still allows proving correctness for optimizers that work at the level of the blocks of the CFG (e.g., super-optimizers [27,11,10] and many rule-based optimizations performed by the Solidity compiler [9]). Considering only stack optimizations, and leaving out memory and storage simplifications and blockchain-specific bytecodes, does not restrict the considered programs, as we work at the smaller block partitions induced by the not handled operations found in the block (splitting into the block before and after). Even in our narrowed setting, the problem is challenging as block-optimizations can include any elimination, reorder and even change of the original bytecodes.

Consider the next block I, taken from a real smart contract [8]. The GASOL optimizer [10], relying on the commutativity of OR and AND, optimizes it to O:

- I: PUSH2 0x100 PUSH1 0x1 PUSH1 0xa8 SHL SUB NOT SWAP1 SWAP2 AND PUSH1 0x8 SWAP2 SWAP1 SWAP2 SHL PUSH2 0x100 PUSH1 0x1 PUSH1 0xa8 SHL SUB AND OR PUSH1 0x5
- 0: PUSH2 0x100 PUSH1 0x1 PUSH1 0xa8 SHL SUB DUP1 NOT SWAP2 PUSH1 0x8 SHL AND SWAP2 AND OR PUSH1 0x5

This saves 11 bytes because (1) the expression SUB(SHL(168,1),256)—that corresponds to "PUSH2 0x100 PUSH1 0x1 PUSH1 0xa8 SHL SUB"—is computed twice; but it can be duplicated if the stack operations are properly made saving 8 bytes; and (2) two SWAPs are needed instead of 5, saving 3 more bytes.

This paper proposes a technique, and a corresponding tool, to automatically verify the correctness of EVM block-optimizations (as those above) on smart contracts using the Coq proof assistant. This amounts to the challenging problem of proving semantic equivalence of two blocks of EVM instructions, which is realized by means of three main components which constitute our main contributions (all formalized and proven correct in Coq): (1) a symbolic interpreter in Coq to symbolically execute the EVM blocks I and O and produce resulting symbolic states S_I and S_0 , (2) a series of simplification rules, which transform S_I and S_0 into equivalent ones S_I' and S_0' , (3) a checker of symbolic states in Coq to decide if two symbolic states S_I' and S_0' are semantically equivalent.

2 Background

The Ethereum VM (EVM) [36] is a stack-based VM with a word size of 256-bits that is used to run the smart contracts on the Ethereum blockchain. The EVM has the following categories of bytecodes: (1) Stack operations; (2) Arithmetic operations; (3) Comparison and bitwise logic operations; (4) Memory and storage manipulation; (5) Control flow operations; (6) Blockchain-specific opcodes,

e.g., block and transaction environment information, compute hash, calls, etc. The first three types of opcodes are handled within our verifier, and handling optimizations on opcodes of types 4-6 is discussed in Sec. 6.

The focus of our work is on optimizers that perform optimizations only at the level of the blocks of the CFG (i.e., intra-block optimizations). A well-known example is the technique called *super-optimization* [24] which, given a loop-free sequence of instructions searches for the optimal sequence of instructions that is semantically equivalent to the original one and has optimal cost (for the considered criteria). This technique dates back to 1987 and has had a revival [29,23] thanks to the availability of SMT solvers that are able to do the search efficiently. We distinguish two types of possible intra-block optimizations: (i) Rule-based optimizations which consist in applying arithmetic/bitwise simplifications (see Fig. 1); and (ii) Stack-data optimizations which consist in searching for alternative stack operations that lead to an output stack with exactly the same data.

The first type of optimizations are applied by the optimizer integrated in the Solidity compiler [9] as rule transformations, and they are also applied by EVM optimizers in different ways. ebso [27] encodes the semantics of arithmetic and bitwise operations in the SMT encoding so that the SMT solver searches for these optimizations together with those of type (ii). Instead, SYRUP [11] and GASOL [10] apply rule-based optimizations in a pre-phase and leave to the SMT solver only the search for the second type of optimizations. This classification of optimizations is also relevant for our approach as (i) will require integrating and proving all simplification rules correct (Sec. 4.2) while (ii) are implicit within the symbolic execution (Sec. 4.1). A block of EVM code that has been subject to optimizations of the two types above is in principle "provable" using our tool.

There is not much work yet on formalizing the EVM semantics in Coq. One of the most developed approaches is [20], which is a definition of the EVM semantics in the Lem [26] language that can be exported to interactive theorem provers like Isabelle/HOL or Coq. According to the comparison in [19], this implementation of EVM "is executable and passes all of the VM tests except for those dealing with more complicated intercontract execution". However, we have decided not to use it for our checker due to three reasons: (a) the generated Coq code from Lem definitions is not "necessarily idiomatic" and thus it would generate a very complex EVM formalization in Coq that would make theorems harder to state and prove; (b) the author of the Lem definition states that "the Coq version of the EVM definition is highly experimental"; and (c) it is not kept up-to-date.

The other most developed implementation of the EVM semantics in Coq that we have found is [21]. It supports all the basic EVM bytecodes we consider in our checker, and looked promising as our departing point. The implementation uses Bedrock Bit Vectors (bbv) [7] for representing the EVM 256-bit values, as we use as well. It is not a full formalization of the EVM because it does not support calling or creation of smart contracts, but provides a function that simulates consequent application of opcodes to the given execution state, call info and Ethereum state mocks. The latter two pieces of information would add complexity and are not needed for our purpose. Therefore, we decided to develop our own EVM

formalization in Coq (presented in Sec. 3) which builds upon some ideas of [21], but introduces only the minimal elements we need to handle the instructions supported by the checker. This way the proofs will be simpler and conciser.

3 EVM Semantics in Coq

Our EVM formalization is a concrete interpreter that executes a block of EVM instructions. For representing EVM words we use EVMWord that stands for the type "word 256" of the bbv library [7]. For representing instructions we use:

Type stack_oper_instr defines instructions that operate only on the stack, i.e., each pops a fixed number of elements and pushes a single value back (see App. B for the full list). Type instr encapsulates this category together with the stack manipulation instruction (PUSH, etc). The type block stands for "list instr".

To keep the framework general, and simplify the proofs, the actual implementation of instructions from <code>stack_op_instr</code> are provided to the interpreter as input. For this, we use a map that associates instructions to implementations:

```
\label{eq:local_control_control} \begin{split} &\operatorname{Inductive\ stack\_operation} := \\ &| \ \operatorname{StackOp}\ (\operatorname{comm}:\ \operatorname{bool})\ (\operatorname{n}:\ \operatorname{nat})\ (\operatorname{f}:\ \operatorname{list\ EVMWord} \to \operatorname{option\ EVMWord}). \\ &\operatorname{Definition\ stack\_op\_map} := \operatorname{map\ stack\_oper\_instr\ stack\_operation}. \end{split}
```

The type stack_operation defines an implementation for a given operation: comm indicates if the operation is commutative; n is the number of stack elements to be removed and passed to the operation; and f is the actual implementation. The type stack_ope_map maps keys of type stack_oper_instr to values of type stack_operation. Suppose evm_add and evm_mul are implementations of ADD and MUL (see App. C), the actual stack operations map is constructed as follows:

In addition, we require that the operations in the map to be valid with respect to the properties that they claim to satisfy (e.g., commutativity), and that when applied to the right number of arguments they should succeed (i.e., do not return None). We refer to this property as valid_stack_op_map.

An execution state (or simply state) includes only a stack (currently we support only stack operations) which is as a list of EVMWord, and the interpreter is a function that takes a block, an initial state, and a stack operations map, and iteratively executes each of the block's instructions:

```
Definition stack := list EVMWord.
Inductive state :=
   | ExState (stk: stack).
Fixpoint concr_int (p: block) (st: state) (ops: stack_op_map): option state := ...
```

The result can be either Some st or None in case of an error which are caused only due to stack overflow. In particular, we are currently not taking into account the amount of gas needed to execute the block. Note that our implementation follows the EVM semantics [36], and we plan to test it using EVM test suite.

4 Formal Verification of EVM-Optimizations in Coq

Two jump-free blocks p1 and p2 are equivalent wrt. to k, if for any initial stack of size k, the executions of p1 and p2 succeed and lead to the same state. Formally:

Note that when concr_int returns None for both p1 and p2, they are not considered equivalent because in the general case they can fail due to different reasons.

An EVM block equivalence checker is a function that takes two blocks, the size of the initial stack, and returns true/false. Its soundness is stated as follows:

Given two blocks p_1 and p_2 , checking their equivalence (in Coq) has the following components: (i) Symbolic Execution (Sec. 4.1): it is based on an interpreter that symbolically executes a block, wrt. an initial symbolic stack of size k, and generates a final symbolic stack. It is applied on both p_1 and p_2 to generate their corresponding symbolic output states S_1 and S_2 . (ii) Rule optimizations (Sec. 4.2): it is based on simplification rules that are often applied by program optimizers, which rewrite symbolic states to equivalent "simpler" ones. This step simplifies S_1 and S_2 to S_1' and S_2' . (iii) Equivalence Checker (Sec. 4.3): it receives the simplified symbolic states, and determines if they are equivalent for any concrete instantiation of the symbolic input stack. It takes into account, for example, the fact that some stack operations are commutative.

4.1 EVM Symbolic Execution in Coq

Symbolic execution takes an initial symbolic state (i.e., stack) $[s_0,\ldots,s_k]$, a block, and a map of stack operations, and generates a final symbolic state (i.e., stack) with symbolic expressions, e.g., $[5+s_0,s_1,s_2]$, representing the corresponding computations. In order to incorporate rule-based optimizations in a simple and efficient way, we want to avoid compound expressions such as $5+(s_0*s_1)$, and instead use temporal fresh variables together with a corresponding map that assigns them to simpler expressions. E.g, the stack $[5+(s_0*s_1),s_2]$ would be represented as a tuple $([e_1,s_2],\{e_1\mapsto 5+e_0,e_0\mapsto s_0*s_1\})$ where e_i are fresh variables. To achieve this, we define the symbolic stack as a list of elements that can be numeric constant values, initial stack variables or fresh variables:

```
Inductive sstack_val : Type :=
```

```
| \  \, \text{Val (val: EVMWord)} \, | \, \, \text{InStackVar (var: nat)} \, | \, \, \text{FreshVar (var: nat)}. Definition sstack := list sstack_val.
```

and the map that assigns meaning to fresh variables is a list that maps each fresh variable to a sstack_val, or to a compound expression:

```
Inductive smap_val : Type :=
    | SymBasicVal (val: sstack_val)
    | SymOp (opcode : stack_op_instr) (args : list sstack_val).
Definition smap := list (nat*smap_val).
```

Finally, a symbolic state is defined as a SymState term where k is the size of the initial stack, maxid is the maximum id used for fresh variables (kept for efficiency), sstk is a symbolic stack, and m is the map of fresh variables.

```
{\tt Inductive\ sstate: Type:=|\ SymState\ (k\ maxid:\ nat)\ (sstk:\ sstack)\ (m:\ smap)}.
```

Example 1 (Symbolic execution). Given $p_1 \equiv$ "PUSH1 0x5 SWAP2 MUL ADD" and $p_2 \equiv$ "PUSH1 0x0 ADD MUL PUSH1 0x5 ADD", symbolically executing them with k=3 we obtain the symbolic states represented by $\mathtt{sst1} \equiv ([e_1', s_2], \{e_1' \mapsto e_0' + 5, e_0' \mapsto s_1 * s_0\})$ and $\mathtt{sst2} \equiv ([e_2, s_2], \{e_2 \mapsto 5 + e_1, e_1 \mapsto e_0 * s_1, e_0 \mapsto 0 + s_0\})$.

Note that we impose some requirements on symbolic states to be valid. E.g., for any element $i \mapsto v$ of the fresh variables map, all fresh variables that appear in v have smaller indices than i. We refer to these requirements as valid_sstate.

Given a symbolic (final) state and a concrete initial state, we can convert the symbolic state into a concrete one by replacing each s_i by its corresponding value, and evaluating the corresponding expressions (following their definition in the stack operations map). We have a function to perform this evaluation that takes the stack operations map as input:

```
Definition eval_sstate (in_st: state) (sst: sstate) (ops: stack_op_map) : option state := ...
```

Our symbolic execution engine is a function that takes the size of the initial stack, a block, a map of stack operations, and generates a symbolic final state:

```
Definition sym_exec (p: block) (k: nat) (ops: stack_op_map) : option sstate := ...
```

Note that we do not pass an initial symbolic state, but rather we construct it inside using k. Also, the result can be None in case of failure (the causes are the same as those of conc_interpreter).

Soundness of sym_{exec} means that whenever it generates a symbolic state as a result, then the concrete execution from any stack of size k will succeed and produce a final state that agrees with the generated symbolic state:

```
Theorem sym_exec_snd:
\forall \; (p:\; block) \; (k:\; nat) \; (ops:\; stack\_op\_map) \; (sst:\; sstate),
valid\_stack\_op\_map \; ops \; \rightarrow
sym\_exec \; p \; k \; ops \; = \; Some \; sst \; \rightarrow
valid\_sstate \; sst \; \land
\forall \; (in\_st:\; state) \; (in\_stk:\; stack),
get\_stack \; in\_st \; = \; in\_stk \; \rightarrow
```

```
length in_stk = k →
∃ (out_st : state),
  concr_int p in_st ops = Some out_st ∧
  eval_sstate in_st sst ops = Some out_st
```

4.2 Simplification Rules

To capture equivalence of programs that have been optimized according to "rule simplifications" (type (i) in Sec. 2) we need to include the same type of simplifications (see Fig. 1) in our framework. Without this, we will capture EVM-blocks equivalence only for "data-stack equivalence optimizations" (type (ii) in Sec. 2).

An optimization function takes as input a symbolic state, and tries to simplify it to an equivalent state. E.g, if a symbolic state includes $e_i \mapsto s_3 + 0$, we can replace it by $e_i \mapsto s_3$. The following is the type used for optimization functions:

```
\texttt{Definition optim} := \texttt{sstate} \rightarrow \texttt{sstate*bool}.
```

Optimization functions never fail, i.e., in the worst case they return the same symbolic state. This is why the returned value includes a Boolean to indicate if any optimization has been applied, which is useful when composing optimizations later. The soundness of an optimization function can be stated as follows:

```
Definition optim_snd (opt: optim): Prop :=
forall (sst: sstate) (sst': sstate) (b: bool),
valid_sstate sst \rightarrow opt sst = (sst', b) \rightarrow
(valid_sstate sst' \rightarrow
forall (st st': state), eval_sstate st sst evm_stack_opm = Some st' \rightarrow
eval_sstate st sst' evm_stack_opm = Some st').
```

So far we have implemented and proven correct the most-used simplification rules of Fig. 1 (see App. A). E.g., there is an optimization function $\operatorname{optimize_add_zero}$ that rewrites expressions of the form E+0 or 0+E to E, and its soundness theorem is:

```
Theorem optimize_add_zero_snd: optim_snd optimize_add_zero.
```

Example 2. Consider again the blocks of Ex. 1. Using optimize_add_zero we can rewrite sst2 to sst2' \equiv ([e_2, s_2], { $e_2 \mapsto 5 + e_1, e_1 \mapsto e_0 * s_1, e_0 \mapsto s_0$ }), by replacing $e_0 \mapsto 0 + s_0$ by $e_0 \mapsto s_0$.

Note that the checker can be easily extended with new optimization functions, simply by providing a corresponding implementation and a soundness proof. Optimization functions can be combined to define *simplification strategies*, which are also functions of type optim. E.g., assuming that we have *basic* optimization functions $f_1,...,f_n$: (1) Apply $f_1,...,f_n$ iteratively such that in iteration i function f_i is applied as many times as it can be applied. (2) Apply each f_i once in some order and repeat the process as many times as it can be applied. (3) Use the simplifications that were used by the optimizer (it needs to pass these hints).

4.3 Stacks Equivalence Modulo Commutativity

We say that two symbolic stacks sst1 and sst2 are equivalent if for every possible initial concrete state st they evaluate to the same state. Formally:

However, this notion of semantic equivalence is not computable in general, and thus we provide an effective procedure to determine such equivalence by checking that at every position of the stack both contain "similar" expressions:

```
Definition eq_sstate_chkr (sst1 sst2: sstate) (ops : stack_op_map) : bool := ...
```

To determine if two stack elements are similar, we follow their definition in the map if needed until we obtain a value that is not a fresh variable, and then either (1) both are equal constant values; (2) both are equal initial stack variables; or (3) both correspond to the same instruction and their arguments are (recursively) equivalent (taking into account the commutativity of operations).

Example 3. eq_sstate_chkr fails to prove equivalence of sst1 and sst2 of Ex. 1, because, when comparing e_2 and e'_1 , it will eventually check if $0 + s_0$ and s_0 are equivalent. It fails because the comparison is rather "syntactic". However, it succeeds when comparing sst1 and sst2' (Ex. 2), which is a simplification of sst2.

This procedure is an approximation of the semantic equivalence, and it can produce false negatives if two symbolic states are equivalent but are expressed with different syntactic constructions. However, it is sound:

Note that we require the stack operations map to be valid in order to guarantee that the operations declared commutative in ops are indeed commutative. In order to reduce the number of false negatives, the simplification rules presented in Sec. 4.2 are very important to rewrite symbolic states into closer syntactic shapes that can be detected by eq_sstate_chkr.

Finally, given all the pieces developed above, we can now define the block equivalence checker as follows:

It symbolically executes p1 and p2, simplifies the resulting symbolic states by applying optimization opt, and finally calls eq_sstate_chkr to check if the states are equivalent. The above checker is sound when opt is sound:

```
Theorem evm_eq_block_chkr_snd: \forall (opt: optim), optim_snd opt \rightarrow eq_block_chkr_snd (evm_eq_block_chkr opt)
```

5 Implementation and Experimental Evaluation

The different components of the tool have been implemented in Coq v8.15.2, together with complete proofs of all the theoretical results (more than 180 proofs in ~7000 lines of Coq code). The code can be found at https://github.com/costa -group/coq-evm/tree/v2023.01. The tool currently includes 15 simplification rules from those of Fig. 1 (see App. A). We have tried our implementation on the outcome of two optimization tools: (1) the standalone GASOL optimizer and, (2) the optimizer integrated within the Solidity compiler solc. For (1), we have already fully automated the communication among the optimizer and checker and have been able to perform a thorough experimental evaluation. While in (2), the communication is more difficult to automate because the CFG of the original program can change after optimization, i.e., it can make cross-block optimization. Hence, in this case, we have needed human intervention to disable intra-block optimizations and obtain the blocks for the comparison (we plan to automate this usage in the future). For evaluating (2) we have used as benchmarks 1, 280 blocks extracted from the smart contracts in the semantic test suite of the solc compiler [6], succeeding to prove equivalence on 1,045 out of them. We have checked that the fails are due to the use of optimization rules not yet implemented by us. Now we describe in detail the experimental evaluation on (1) for which we have used as benchmarks 147, 798 blocks belonging to 96 smart contracts (see App. D).

GASOL allows enabling/disabling the application of simplification rules of Fig. 1, and choosing an optimization criteria: GAS consumption or bytes SIZE (of the code) [10]; combining these parameters we obtain 4 different sets of pairsof-blocks to be verified by our tool. From these blocks, we consider only those that were actually optimized by GASOL, i.e., the optimized version is syntactically different from the original one. In all the cases, the average size of blocks is 8 instructions. Table 5.1 summarizes our results, where each row corresponds to one setting out of the 4 mentioned above: Column 1 includes the optimization criteria; Column 2 indicates if rule simplifications were applied by GASOL; Column 3 indicates how many pairs-of-blocks were checked; Columns 4-7 report the results of applying 2 versions of the checker, namely CHKR corresponds to the checker that only compares symbolic states and CHKR's corresponds to the checker that also applies all the implemented rule optimizations iteratively as much as they can be applied (see Sect. 4.2). For each we report the number of instances it proved equivalent and the total runtime in seconds. The experiments have been performed on a machine with an Intel i7-4790 at 3.60 GHz and 16GB of RAM.

For sets in which GASOL does not apply simplification rules (marked with \times), both CHKR and CHKR^s succeed to prove equivalence of all blocks. When simplifications are applied (marked with \checkmark), CHKR^s succeeds in 99% of the blocks while CHKR ranges from 63% for GAS to 99% for SIZE. This difference is due to the fact that GASOL requires the application of rules to optimize more blocks

	#blocks	CHKR		CHKR ^s	
SIMP		Yes	Time	Yes	Time
GAS ×	36624 43228	36624	2.60	36624	11.76
<mark>ය</mark> <	43228	27149	4.69	43109	14.09

	#blocks CHKR		KR	\mathbf{CHKR}^{s}	
SIMP		Yes	Time	Yes	Time
SIZE	35754 32192	35754 31488	$2.57 \\ 2.50$	35754 31798	12.59 12.17

Table 5.1. Summary of experiments using GASOL.

wrt. GAS ($\sim 37\%$ of the total) than wrt. SIZE ($\sim 1\%$). Moreover, all the blocks that CHKR^s cannot prove equivalent have been optimized by GASOL using rules which are not currently implemented in the checker, so we predict a success rate of 100% when all the rules in Fig. 1 are integrated. Regarding time, CHKR^s is 3–5 times slower than CHKR because of the overhead of applying rule optimizations, but it is still very efficient (all 147.798 instances are checked in 50.61 seconds). As a final comment, thanks to the checker we found a bug in the parsing component of GASOL that has been reported to its developers.

6 Conclusions, Related and Future Work

Our work provides the first tool able to formally verify the equivalence of jump-free EVM blocks and has required the development of all components within the verification framework. The implementation is not tied to any specific tool and could be easily integrated within any optimization tool. Ongoing work focuses on handling memory and storage optimizations. This extension needs to support the execution of memory/storage operations at the level of the concrete interpreter, and design an efficient data structure to represent symbolic memory/storage. Full handling of blockchain-specific opcodes is straightforward, it only requires adding the corrsponding implementations to the stack operations map evm_stack_opm. A more ambitious direction for future work is to handle cross-block optimizations.

There are two approaches to verify program optimizations, (1) verify the correctness of the optimizations and develop a verified tool, e.g., this is the case of optimizations within the CompCert certified compiler [22] and a good number of optimizations that have been formally verified in Coq [25,17,30,31,12], (2) or use a translation validation approach [32,33,34,18] in which rather than verifying the tool, each of the compiled/optimized programs are formally checked to be correct using a verified checker. We argue that translation validation [32] is the most appropriate approach for verifying EVM optimizations because: (i) EVM compilers (together with their built-in optimizers) are continuously evolving to adjust to modifications in the rather new blockchain programming languages, (ii) existing EVM optimizers use external components such as SMT solvers to search for the optimized code and verifying an SMT solver would require a daunting effort, (iii) we aim at generality of our tool rather than restricting ourselves to a specific optimizer and, as already explained, the design of our checker has been done having generality and extensibility in mind, so that new optimizations can be easily incorporated. Finally, it is worth mentioning the KEVM framework [19], which in principle could be the basis for verifying optimizations as well. However, we have chosen to develop it in Coq due to its maturity.

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A Rule simplifications

Fig. 1 includes rule simplifications that are applied by tools like GASOL and the Solidity compiler solc. Those rules integrated in our checker are marked with *

```
\mathbf{(1*)} \quad \mathbf{OP}(\mathbf{X_{int}}, \mathbf{Y_{int}}) = \mathbf{eval}(\mathbf{OP}, \mathbf{X_{int}}, \mathbf{Y_{int}})
                                              (34*) ISZERO(ISZERO(ISZERO(X))) = ISZERO(X)
\mathbf{(2*)} \quad \mathbf{OP}(\mathbf{X_{int}}) = \mathbf{eval}(\mathbf{OP}, \mathbf{X_{int}})
     ADD(X, 0) = X
(3*)
                                              (35) ISZERO(XOR(X,Y)) = EQ(X,Y)
      SUB(X,0) = X
                                                   ISZERO(ISZERO(GT(X,Y))) = GT(X,Y)
(4)
                                              (36)
(5*) \quad \mathbf{SUB}(\mathbf{X}, \mathbf{X}) = \mathbf{0}
                                              (37)
                                                    ISZERO(ISZERO(LT(X,Y))) = LT(X,Y)
(6*)
     MUL(X, 0) = 0
                                                   ISZERO(ISZERO(EQ(X,Y))) = EQ(X,Y)
(7*)
     MUL(X, 1) = X
                                              (39)
                                                   SHL(X,0) = 0
(8)
      MUL(SHL(X,1),Y) = SHL(X,Y)
                                              (40)
                                                   SHL(0,X) = X
(9)
      MUL(X, SHL(Y, 1)) = SHL(Y, X)
                                              (41) SHR(0, X) = X
(10) DIV(X, X) = 1
                                              (42) SHR(X,0) = 0
(11*) DIV(X, 1) = X
                                              (43*) \mathbf{NOT}(\mathbf{NOT}(\mathbf{X})) = \mathbf{X}
(12) DIV(X,0) = 0
                                              (44) XOR(X, X) = 0
(13) DIV(X, SHL(Y, 1)) = SHR(Y, X)
                                              (45)
                                                   XOR(X,0) = X
                                                  XOR(X, XOR(X, Y)) = Y
(14) \quad MOD(X,1) = 0
                                              (46)
(15) \quad MOD(X, X) = 0
                                              (47*) \ OR(X,0) = X
                                              (48) \quad OR(2^{256} - 1, X) = 2^{256} - 1
(16) MOD(X, 0) = 0
(17) EXP(X,0) = 1
                                              (49) \quad OR(X, X) = X
(18) EXP(X, 1) = X
                                              (50) OR(X, AND(X, Y)) = X
(19) EXP(1, X) = 1
                                                   OR(OR(X,Y),Y) = OR(X,Y)
(20) EXP(0,X) = ISZERO(X)
                                                   OR(OR(Y, X), Y) = OR(Y, X)
                                                   OR(X, NOT(X)) = 2^{256} - 1
(21) EXP(2, X) = SHL(X, 1)
                                              (53)
                                              (54)
                                                   AND(X,0) = 0
(22) GT(0,X) = 0
(23*) \mathbf{GT}(1, \mathbf{X}) = \mathbf{ISZERO}(\mathbf{X})
                                              (55) \quad AND(X,X) = X
                                              (56) AND(2^{256} - 1, X) = X
(24) \quad GT(X,X) = 0
(25) LT(X,0) = 0
                                              (57*) AND(AND(X,Y),Y) = AND(X,Y)
(26*) LT(X,1) = ISZERO(X)
                                              (58*) AND(AND(Y, X), Y) = AND(Y, X)
(27) LT(X,X) = 0
                                              (59) AND(X, OR(X, Y)) = X
(28) EQ(X,X) = 1
                                              (60) AND(X, NOT(X)) = 0
                                              (61) AND(ORIGIN, 2^{160} - 1) = ORIGIN
(29*) EQ(X,0) = ISZERO(X)
                                              (62) AND(CALLER, 2^{160} - 1) = CALLER
(30) EQ(1, ISZERO(X)) = ISZERO(X)
                                                   \overrightarrow{AND(ADDRESS}, 2^{160} - 1) = \overrightarrow{ADDRESS}
(31) ISZERO(SUB(X,Y)) = EQ(X,Y)
                                              (63)
                                                    \overrightarrow{AND(COINBASE}, 2^{160} - 1) = COINBASE
(32) \quad ISZERO(GT(X,0)) = ISZERO(X)
                                              (64)
(33) ISZERO(LT(0,X)) = ISZERO(X)
                                              (65)
                                                   BALANCE(ADDRESS) = SELFBALANCE
```

Fig. 1. Simplification rules

B Supported Instructions

In Sec. 3 we have discussed a limited number of instructions that are included in the type stack_op_instr. Next we overview the full list of supported instructions. The following stack operations are supported in the checker:

ADD	MUL	NOT	SUB	DIV	SDIV	MOD
SMOD	ADDMOD	MULMOD	EXP	SIGNEXTEND	LT	GT
SLT	SGT	EQ	ISZERO	AND	OR	XOR
BYTE	SHL	SHR	SAR			

They all perform computations that depend only on values stored on the stack, and the result is pushed again to the stack. In addition, in order to increase the set of benchmarks that we can handle, the following are also supported, even though they depend on values stored in the memory/store/contract/etc, in a sound way:

SHA3	KECCAK256	ADDRESS	BALANCE	ORIGIN
CALLER	CALLVALUE	CALLDATALOAD	CALLDATASIZE	CODESIZE
GASPRICE	EXTCODESIZE	RETURNDATASIZE	EXTCODEHASH	BLOCKHASH
COINBASE	TIMESTAMP	NUMBER	DIFFICULTY	GASLIMIT
CHAINID	SELFBALANCE	BASEFEE	SLOAD	MLOAD
PC	MSIZE	GAS		

The support is done by corresponding implementations that always return 0. This is sound for now since (1) they are not used in rule simplifications, and thus they are never executed; and (2) we do not have any instruction that modifies the memory/store. Recall that when comparing symbolic states, if two calls to the same instruction are compared then we require their arguments to be equal and we do not inspect the returned value. For now, in the implementations, they are defined as stack_op_instr but this will change once other instruction categories are formalized.

C Missing code

```
Definition evm_add (args: list EVMWord) : option EVMWord :=
match args with

| [a; b] \Rightarrow Some (wplus a b) (* wplus is part of the bbv library *)

| _ \Rightarrow None
end.
```

```
Definition stack_op_map_comm (ops: stack_op_map) : Prop :=

∀ (instr : stack_oper_instr) (f: list EVMWord → option EVMWord),
ops instr = Some (StackOp true 2 f) →

∀ (a b: EVMWord), f [a;b] = f [b;a].

Definition coherent_stack_op_map (ops: stack_op_map) : Prop :=
```

```
\label{eq:committee} \begin{array}{l} \forall \; (\texttt{instr:} \; \texttt{stack\_op\_instr}) \; (\texttt{comm:} \; \texttt{bool}) \; (\texttt{n:} \; \texttt{nat}) \\ (\texttt{f:} \; \; \texttt{list} \; \texttt{EVMWord} \rightarrow \texttt{option} \; \texttt{EVMWord}), \\ \texttt{ops} \; \; \texttt{instr} \; = \; \texttt{Some} \; (\texttt{StackOp} \; \texttt{comm} \; \texttt{n} \; \texttt{f}) \rightarrow \\ \forall \; (\texttt{l:} \; \; \texttt{list} \; \texttt{EVMWord}), \\ \texttt{length} \; 1 = \mathsf{n} \rightarrow \exists \; (\texttt{v:} \; \texttt{EVMWord}), \; \texttt{f} \; 1 = \; \texttt{Some} \; \texttt{v}. \\ \\ \texttt{Definition} \; \texttt{valid\_stack\_op\_map} \; (\texttt{ops:} \; \texttt{stack\_op\_map}) : \; \texttt{Prop} := \\ \texttt{stack\_op\_map\_comm} \; \texttt{ops} \; \land \; \texttt{coherent\_stack\_op\_map} \; \texttt{ops} \end{array}
```

D Smart contracts used in the experiments

For the experimental evaluation we have extracted all the blocks in the following 96 smart contracts from the Ethereum blockchain. We identify the smart contracts by their addresses.

- $1. \ 0 \times 0621213b273bff05d679d9b1c68ec18cf989168f$
- 2. 0x0edc5ac3da3df2e4643aca1a777ca9eb6656117a
- 3. 0x0f066b014adb057cdfc6c587965fbaa14151dfa5
- $4. \ 0x100739d55a4e8361dcca7e872426c4b6aadeb201$
- 5. 0x16c19aaae850bb0282b38686fb071fe37edecf1f
- $6. \ 0x16d1884381d94b372e6020a28bf41bbabe8c1f26 \\$
- 7. 0x1c52b09ccddd1b6999400b038c7e0680eaf03dcd
- 8. 0x1Ee8923Db533Ecb7A4650cCc8829D6F114D718f9
- 9. 0x269028c988db0e6786de1f4ff66af7c033d0f6c8
- $10. \ 0x2ccc239e97d01ad4c39a323327bc1a1f4cb43076$
- $11. \ 0x2e12AE85aF4121156F62ad4D059415C746fe615c$
- 12. 0x34662bf3ad9b3a70ea5b46ad81f4e9cab4d89a7f
- 13. 0x359651fb6636cb650Fa47F11C9D35533BbFF8158
- $14. \ 0x3948b7b6b8812439ddcbc8fa42cac8e213191792$
- 15. 0x3ae30bb991be0d54fddfedc7d6556e20daa97c71
- 16. 0x3e456b66425f02bfe3896c1cc3b8513ff660b4bf
- 17. 0x4152e8133d79279881013789100246a907884b9e
- $18. \ 0x4226cac9567e991f956f644b656ce4aa0599c63e$
- 19. 0x44f8217a9dbb45ef2491da6aa18826bd6ded7847
- $20. \ 0x450f184242894d068a71d3abfa296a73df1e192c$
- $21. \ 0x4757388aa7e3490106092bde16c23e2858c7d405$
- 22. 0x47B51F81E03fB068d776CcB78b08F59e5256B944
- 23. 0x49173F2BF921Ce4124A8C6aBad3c5875Ff40D951
- $24. \ 0x49566ab7ef0d4da06a3117e9e4fb3e9947abaf96$
- 25. 0x4d2d88d73ab4062d61b1eb68b5808b9176cef271
- 26. 0x4d37D0aB328e1D449Ea8CFc3b0B7364B398c41E0
- 27. 0x4E4bd1f64232450bEa37c4CB76D4b4cda3d46DAa
- 28. 0x4f73c17195d0f77c1fc4175345b9251a9fb21849
- $29. \ 0x4f89a0d9d868a39ec7024828dcaaae140a1a7ff3$
- 30. 0x5036f390F631f66284253864aE351B0297E32f03
- $31. \ 0x50b6c438f108b5c0145142f54d538e704c55995b$

- 32. 0x54adf7604d25ac9476fc467e93dfdb29af1077ee
- $33. \ 0x58760b75093a8462eb2eab2c5769ba5c0b18fa68$
- 34. 0x5d2fdd14e44b090f2eef03c715d414039f86d7bd
- 35. 0x60e600a4d09297f9e9bb6eb90373f48e7830e69c
- 36. 0x6365303A5E1C1327b36bDa8C22440be94eCCbcA1
- 37. 0x64b88f10faf1603b70fb7370a00c43369f329515
- $38. \ 0x697720ee431148a586a546551de6c4d575e4d8d0$
- 39. 0x6cd5a65e85c9603df74d4311d76145820556548a
- 40. 0x6e53a6441b24cb773adcc6e6f9d43e956e7c9a6e
- $41. \ 0x70001ba1ba4d85739e7b6a7c646b8aba5ed6c888$
- 42. 0x702197775Ab2B462Af51Ba11b38d103AaA0bb443
- 43. 0x72BD2930663b30dBA3cd362bc1f8C2251E24C73A
- 44. 0x766a339751Df1705364D961b4f7f87309F210355
- 45. 0x7a741d7ff3da76d722fa4a37455f099efd0ef168
- **46.** 0x7bd251d43d8ee259acde7788ec93b7f3d6626dd2
- $47. \ 0x7dDA9F944c3Daf27fbe3B8f27EC5f14FE3fa94BF$
- 48. 0x7F197F94cA6e57Fd983cE0fa29710cfA3b842bf8
- $\mathbf{49.}\ \ 0 \\ \mathbf{x} \\ 89872650 \\ \mathbf{fa} \\ 1 \\ \mathbf{a} \\ 391 \\ \mathbf{f} \\ 58 \\ \mathbf{b} \\ 4e \\ 144222 \\ \mathbf{b} \\ \mathbf{b} \\ 02e \\ 44d \\ \mathbf{b} \\ 7e \\ 3b \\ \mathbf{b} \\ \mathbf{c} \\$
- 50. 0x8EfbD976709c2bD46bdaf0c3Db83E875F1451BAE
- $51. 0 \times 8 + 693895 \times 64654 \times 6377 \times 6377 \times 61565 \times 646948$
- 52. 0x8f3b62dd6a9bf905516f433c214753934b337e05
- 53. 0x90f24a2432a8b2e87b5a2026855181317890d129
- $54. \ 0x949205a8e58bd1e5eb043c6379d1e7564a85039a$
- 55. 0x94a79038D97e22AC47C9Aa41624f948BDd7ac27D
- 56. 0x99E2C293A8A6c3dAE6A591CEA322D0c3Cd231B2C
- 57. 0xa403f555e419e56F49ba90022f7E7d0d3e86522D
- 58. 0xa7b30042c7e798d0be8e466bf879388acddc526f
- 59. 0xaa30979b30523bff7ca2ba434d126d15ad5b0905
- 60. 0xAa7B19b68a1da16f272564e74b0e99f969c4DF6a
- 61. 0xAbF18841Dca279a030bd9A9122F4460Da57ad547
- 62. 0xAbf52Fc6e5C0e6E44Daac7C6ca79498302D9B0CA
- 63. 0xb4e2ebaf639fd03aebe85bd0960b49ade9879b0f
- 64. 0xb4feb1f99fc9e2688729fc899e1ee3631bbebded
- 65. 0xb5615b9799427280cbc34a33233ef59b6409a711
- 66. 0xb595e208833164d43a08ce529acc2b803d33c30e
- $67. \ 0xb6105c0fa743290f94da9bf304ac45c19f4b2851$
- 68. 0xb8ec5b27de7d971d74e8531baa27853cffdfae1d
- $\mathbf{69.}\ \ 0 \\ \mathbf{x} \\ \mathbf{b} \\ \mathbf{b} \\ \mathbf{4} \\ \mathbf{d} \\ \mathbf{1} \\ \mathbf{f} \\ \mathbf{743} \\ \mathbf{a} \\ \mathbf{8} \\ \mathbf{b} \\ \mathbf{b} \\ \mathbf{a} \\ \mathbf{6318} \\ \mathbf{c} \\ \mathbf{821a7} \\ \mathbf{e} \\ \mathbf{9cf1d632c96}$
- $70.\ 0xbdafddc47d1cbac27f80a918908922aa6bf4b5bc$
- 71. 0xbdf9d5752ec89a3b7c3b7ffe31f5bd565016c221
- $72. \ 0xc581bced4dedab50e8bfdcc67b2a36b92e013d78$
- 73. 0xcbdbc7c264c1abff6646bdd5ba13f1664823b0cd
- 74. 0xcc07e50a953c8c61f5dc077ed171e46210e9783e
- 75. 0xcCFFC73347B05cBDCCe7c3de2a0AdEcDAa8AEf51
- 76. 0xcD097cdB473286a10Cf19CbA9597E4400e8B6943
- $77. \ 0xcfc131c7810f9f7ec859bd3dd020bdb4bb06a5a8$

- $78. \ 0xd2947e1e2ea5c4cd14aaa2b7492549129b087daa$
- 79. 0xda44b167ca409b7fc51ccbd6ef3338b8e19999a8
- $80. \ 0xde1972989f633f10b6e6dc581b785c4618aa8490$
- 81. 0xdfd5235a6d3e184ba27307d7d21ae9b425ff4e6d
- $82. \ 0xe45D283123607B7D97856d49C965faa40542BA94$
- $\textbf{83.}\ \ 0 \\ \text{xe} \\ 7 \\ \text{a} \\ 2241 \\ \text{e} \\ 92 \\ \text{c} \\ 7 \\ \text{b} \\ 7299452 \\ \text{e} \\ 63 \\ \text{d} \\ 53 \\ \text{a} \\ f6692 \\ \text{d} \\ \text{fcd} \\ 0367 \\$
- $84. \ 0 \\ xe8d2f4b9edbb0244167339c3a8daa6d82d959e72$
- 85. 0xEadC2a6fff036C12e62A74392d4c6CA77A5Ea007
- $\textbf{86.}\ \ 0 \\ \textbf{xeb} \\ 453 \\ \textbf{a} \\ 070 \\ \textbf{c} \\ 20 \\ \textbf{e} \\ 79 \\ \textbf{ff} \\ 148 \\ \textbf{e} \\ 0506 \\ \textbf{b} \\ \textbf{d} \\ 02 \\ \textbf{c} \\ 30 \\ \textbf{b} \\ 577 \\ \textbf{a} \\ \textbf{f} \\ 43 \\ \textbf{e} \\ \textbf{e} \\ \textbf{f} \\ \textbf{e} \\ \textbf{e}$
- 87. 0xEf78B55bD7bC090F809535f3B32Bcf1E050815df
- $88. \ 0xF0B0ccED14b2d1D47C351F5Bc0B33AA79470997e$
- $89. \ 0xf1cb8f9738adff8c280d6eae8e2285a839b79f80$
- 90. 0xF2281cA8693B1d35D7a73700909ec8535A57156D
- $91. \ 0xf508bda527d4ef9db712eb0100f1cd8f573bbe88$
- 92. 0xf66ff968773e45dad3e1ac13ffbb63fae0eb1624
- $93. \ 0xf7a84edAc5539b75AFaaA04f1103dBf9Db4b09c6$
- 94. 0xfa1c9bf3de714059b3c019facdcaef785cab098e
- $\mathbf{95}. \ 0 \\ \text{xfc} \\ 21969625 \\ \text{ae} \\ 8933 \\ \text{e} \\ 85 \\ \text{b} \\ 49 \\ \text{df} \\ 3 \\ \text{cc} \\ 28 \\ \text{aa} \\ 7092 \\ \text{fcfc} \\ 70 \\ \text{e} \\ 70 \\ \text{e} \\ 70 \\ \text{e} \\ 70 \\ \text{e} \\ 10 \\ 10 \\ \text{e} \\ 10 \\ 10 \\ \text{e} \\ 10 \\ 10 \\ \text{e} \\$
- 96. 0xfeff9661617cbba5a2ed3a69000f4bf1e266be71