Computational Logic

Introduction to Logic Programming

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Programs

Terminology

- a Horn clause without negated literals is a fact
- a Horn clause which has a non-negated literal and the other literals negated is a *rule*
 - the non-negated literal is the head
 - the sequence of negated literals is the body
- a set of rules with the same head predicate p is a procedure, whose name is p
- a logic program is a set of procedures

Rule syntax

Queries

Execution

- a goal is a Horn clause with all literals negated
- the deduction whose correctness has to be verified has the program as premise, and the goal as conclusion
- the *execution* of a logic program on a given goal consists of verifying if the goal can be deduced from the program, and, if it can, computing the values of the goal variables which give the answer
- SLD resolution is used, with the goal as the initial goal clause
- most implementations of this kind of languages use a computation rule which follows the order in which rules are written (top-down) and depth search with *backtracking*
 - infinite loops may occur

Query syntax $\neg B_1 \lor \neg B_2$ $B_1 \land B_2$ $\leftarrow B_1, B_2$.?- B1,B2.

Properties

Limitations: some rules are not allowed

- $P_1 \wedge P_2 \rightarrow \neg Q$
 - implication cannot end in something which is not true
- $P_1 \wedge P_2 \rightarrow Q_1 \vee Q_2$
 - it is not possible to state a disjunction
- $P_1 \land \neg P_2 \to Q$
 - premises must be true

Negation

- complete knowledge about the universe is assumed (closed-world hypothesis)
- negation is simulated by negation as failure: what cannot be proven is false
 - dangerous, but useful in finite domains

Execution

To prove a literal C

- ${\ensuremath{\mathfrak{O}}}$ repeat until the top of ${\ensuremath{\mathcal{S}}}$ is an answer literal and no further steps can be preformed
 - **9** pop from S a literal L
 - 2 choose a rule or fact whose head unifies with $L (MGU \alpha)$
 - $\bullet\,$ push in ${\cal S}$ the literals (ordered) of the body of the rule
 - $\bullet \ \mbox{apply} \ \alpha$ to the complete ${\mathcal S}$
 - $\bullet\,$ rename variables in ${\cal S}$
 - () if not possible, fail

Backtracking

When the choice of the rule whose head unifies with L comes to be impossible, the search must go *back* to a *choice point* above in the tree and take another literal L'

Example

Parents and grandparents

- 1 father(a,b).
- 2 mother(b,c).
- 3 grandparent(X,Z) :- parent(X,Y), parent(Y,Z).
- 4 parent(X,Y)
- :- father(X,Y).
- 5 parent(X,Y) :- mother(X,Y).

• who is the grandparent of c? ?- grandparent(X,c). grandparent(X,c), ans(X). $\rightarrow 3, \{X_3/X, Z_3/C\}$ parent(X,Y3), parent(Y3,c), ans(X) $\rightarrow 4, \{X_4/X, Y_4/Y_3\}$ father(X,Y3), parent(Y3,c), ans(X) $\rightarrow 1, \{X/a, Y_3/b\}$ parent(b,c), ans(a) $\rightarrow 4, \{X'_4/b, Y'_4/c\}$ father(b,c), ans(a) $\rightarrow 4, \{X'_4/b, Y'_4/c\}$ mother(b,c), ans(a) $\rightarrow 7iil, 5, \{X_5/b, Y_5/c\}$ mother(b,c), ans(a) $\rightarrow 2, \{\}$

Example

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• who is the grandchild of a? ?- grandparent(a,X).

grandparent(a,X), ans(X). \rightarrow 3, \{X_3/a, Z_3/X\}

parent(a,Y3), parent(Y3,X), ans(X) \rightarrow 4, \{X_4/a, Y_4/Y_3\}

father(a,Y3), parent(Y3,X), ans(X) \rightarrow 1, \{Y_3/b\}

parent(b,X), ans(X) \rightarrow 4, \{X'_4/b, Y'_4/X\}

father(b,X), ans(X) \rightarrow 4, \{X'_4/b, Y'_4/X\}

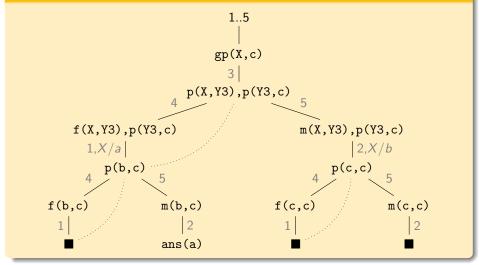
mother(b,X), ans(X) \rightarrow fail, 5, \{X_5/b, Y_5/X\}

mother(b,X), ans(X) \rightarrow 2, \{X/c\}

ans(c)
```

Example

Parents and grandparents



Operational

- the program defines a series of *procedures* (the heads) using *calls* to other procedures (the literals in the body)
- the goal is a series of calls to be executed sequentially (in the order they are written), with the possibility to *go back*

Declarative

- the program declares the information about the problem to be solved
- the problem is formulated as a question
- the task is proving that the question is a correct conclusion of the premises (program)
- an execution is a proof

Operational vs. declarative

Applications

- arithmetics (reversible)
- data structures, recursion
- database systems
- search problems
- rule-based expert systems

Ads

The CLIP group

- the Computational logic, Languages, Implementation, and Parallelism Laboratory
- http://www.clip.dia.fi.upm.es/
- http://www.clip.dia.fi.upm.es/Software/Ciao/